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CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Advanced Level

MARK SCHEME for the May/June 2014 series

9709 MATHEMATICS

9709/33

Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2014 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



Page 2	Mark Scheme	Syllabus	Paper	
	GCE A LEVEL – May/June 2014	9709	33	

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol
 [↑] implies that the A or B mark indicated is allowed for work correctly following
 on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
 A and B marks are not given for fortuitously "correct" answers or results obtained from
 incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Mark Scheme	Syllabus	Paper	
	GCE A LEVEL – May/June 2014	9709	33	

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a "fortuitous" answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through \nabla" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR −2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

	Page 4	Mark Scheme Sylla	bus Pape	er
		GCE A LEVEL – May/June 2014 970		
	Use law of	The logarithm of a quotient or product or $2 = \log_{10} 100$	M1	
		egarithms and obtain $x + 9 = 100x$, or equivalent	A1	
		wer $x = \frac{1}{11}$	A1	3
		11		
		rect unsimplified version of the x or x^2 or x^3 term	M1	
		ct first two terms $1 - x$	$\begin{array}{c} A1 \\ A1 + A1 \end{array}$	
	Obtain the next two terms $2x^2 - \frac{14}{3}x^3$			4
	[Symbolic	binomial coefficients, e.g. $\binom{-\frac{1}{3}}{3}$ are not sufficient for the M mark.]		
	(i) Use ta	$an(A \pm B)$ formula and obtain an equation in $tan x$	M1	
	Using	$\tan 60^{\circ} = \sqrt{3}$, obtain a horizontal equation in $\tan x$ in any correct form	A1	
		ce the equation to the given form	A1	3
((ii) Solve	the given quadratic for tan x	M1	
`	Obtain	n a correct answer, e.g. $x = 21.6^{\circ}$	A1	
		n a second answer, e.g. $x = 128.4^{\circ}$, and no others	A1	3
		re answers outside the given interval. Treat answers in radians as a misrea 7, 2.24).]	ıu	
	(i) Consi	der sign of $x-10/(e^{2x}-1)$ at $x = 1$ and $x = 2$	M1	
		elete the argument correctly with correct calculated values	A1	2
((ii) State	or imply $\alpha = \frac{1}{2} \ln(1 + 10/\alpha)$	B1	
	Rearra	ange this as $\alpha = 10/(e^{2\alpha} - 1)$ or work <i>vice versa</i>	B1	2
(i		ne iterative formula correctly at least once	M1	
		n final answer 1.14	A1	
		sufficient iterations to 4 d.p. to justify 1.14 to 2 d.p., or show there is a si interval (1.135, 1.145)	gn change A1	3
	G ,		D.I.	
	-	ariables correctly and attempt integration of at least one side m in the form $a\sqrt{(2x+1)}$	B1 M1	
		·	B1	
	Express $1/(\cos^2\theta)$ as $\sec^2\theta$			
		n of the form $k \tan \theta$ constant, or use limits $x = 0$, $\theta = \frac{1}{4}\pi$ in a solution with terms $a\sqrt{(2x+1)}$ a	M1 and $k \tan \theta$	
	evaluate a ak≠0	constant, or use mints $x = 0$, $v = \frac{1}{4}n$ in a solution with terms $a\sqrt{(2x+1)}$ and	and κ tan θ , M1	
		rect solution in any form, e.g. $\sqrt{(2x+1)} = \frac{1}{2} \tan \theta + \frac{1}{2}$	A1	
		,		7
	Kearrange	and obtain $x = \frac{1}{8} (\tan \theta + 1)^2 - \frac{1}{2}$, or equivalent	A1	7

		J	GCE A LEVEL – May/June 2014	9709	33	
6		Obtain correct derivative of RHS in any form Obtain correct derivative of LHS in any form			B1 B1	
	Set	$\frac{\mathrm{d}y}{\mathrm{d}x}$ equal t	o zero and obtain a horizontal equation		M1	
			ct equation, e.g. $x^2 + y^2 = 1$, from correct work		A1	
			in the curve equation, or otherwise, obtain an equation in x	x^2 or y^2	M1	
		$tain x = \frac{1}{2}\sqrt{3}$	3		A1	_
	Obt	$tain y = \frac{1}{2}$			A1	7
7	(a)	EITHER:	Multiply numerator and denominator by $1 - 4i$, or equival	ent, and use $i^2 = -$		
			Simplify numerator to $-17 - 17i$, or denominator to 17 Obtain final answer $-1 - i$		A1 A1	
		OR:	Using $i^2 = -1$, obtain two equations in x and y, and solve	for <i>x</i> or for <i>y</i>	M1	
			Obtain $x = -1$ or $y = -1$, or equivalent	,	A1	
			Obtain final answer −1 − i		A1	3
	(b)		v a point representing 2 + i in relatively correct position		B1	
			v a circle with centre 2 + i and radius 1 v the perpendicular bisector of the line segment joining i and	1 2	B1√ B1	
			the correct region		B1	4
		(ii) State requi	or imply that the angle between the tangents from the o	rigin to the circle	is M1	
		_	in answer 0.927 radians (or 53.1°)		A1	2
8	(i)	Use a cor	rect method for finding a constant		M1	
			the of $A = 3$, $B = 3$, $C = 0$		A1	
			second value shird value		A1 A1	4
	(ii)	Integrate	and obtain term $-3\ln(2-x)$		B1 √	
		Integrate	and obtain term of the form $k \ln(2 + x^2)$		M1	
		Obtain ter	$rm \frac{3}{2} ln(2+x^2)$		A1√	
			e limits correctly in an integral of the form $a \ln(2-x) + b \ln(x)$	$(2+x^2)$, where ab	≠ 0 M1	
		Obtain gi	ven answer after full and correct working		A1	5
9	(i)		e for x and dx throughout using $u = \sin x$ and $du = \cos x dx$, o	r equivalent	M1	
			tegrand e^{2u}		A1	
			definite integral $\frac{1}{2}e^{2u}$		A1	
			is $u = 0$, $u = 1$ correctly, or equivalent		M1	_
		Obtain an	swer $\frac{1}{2}(e^2-1)$, or exact equivalent		A1	5

Mark Scheme

Syllabus

Paper

Page 5

Page 6		Mark Scheme	Syllabus	Paper	
	Ŭ	GCE A LEVEL – May/June 2014	9709	33	
(ii)	Use chain	rule or product rule		M1	
	Obtain co	rrect terms of the derivative in any form, e.g. $2\cos x e^{2\sin x}$	$\cos x - e^{2\sin x} \sin x$	A1 + A1	
	Equate derivative to zero and obtain a quadratic equation in sin x		M1		
		Solve a 3-term quadratic and obtain a value of x		M1	
	Obtain an	swer 0.896		A1	6
10 (i)	Express g	general point of <i>l</i> in component form, e.g. $(1+3\lambda, 2-2\lambda, -1+3\lambda, -1+3\lambda, 2-2\lambda, -1+3\lambda, -1+$	- 2 <i>λ</i>)	B1	
	Substitute	e in given equation of p and solve for λ		M1	
		nal answer $-\frac{1}{2}\mathbf{i} + 3\mathbf{j} - 2\mathbf{k}$, or equivalent, from $\lambda = -\frac{1}{2}$		A1	3
(ii)	State or in	mply a vector normal to the plane, e.g. $2\mathbf{i} + 3\mathbf{j} - 5\mathbf{k}$		В1	
	Using the	e correct process, evaluate the scalar product of a directio	n vector for l and	l a	
	normal fo			M1	
		correct process for the moduli, divide the scalar product by	by the product of t		
		ad find the inverse sine or cosine of the result		M1	
	Obtain an	swer 23.2° (or 0.404 radians)		A1	4
(iii)	EITHER:	State $2a + 3b - 5c = 0$ or $3a - 2b + 2c = 0$		B1	
, ,		Obtain two relevant equations and solve for one ratio, e.g.	a:b	M1	
		Obtain $a : b : c = 4 : 19 : 13$, or equivalent		A1	
		Substitute coordinates of a relevant point in $4x + 19y + 13$.	z = d, and evaluate		
	OD1	Obtain answer $4x + 19y + 13z = 29$, or equivalent		A1	
	<i>OR</i> 1:	Attempt to calculate vector product of relev	ant vectors, e	.g.	
		$(2i + 3j - 5k) \times (3i - 2j + 2k)$ Obtain two correct components of the product		M1 A1	
		Obtain two correct components of the product Obtain correct product, e.g. $-4i - 19j - 13k$		A1	
		Substitute coordinates of a relevant point in $4x + 19y + 13$.	z = d	M1	
		Obtain answer $4x + 19y + 13z = 29$, or equivalent	2	A1	
	OR2:	Attempt to form a 2-parameter equation with relevant vector	tors	M1	
		State a correct equation, e.g. $\mathbf{r} = \mathbf{i} + 2\mathbf{j} - \mathbf{k} + \lambda(2\mathbf{i} + 3\mathbf{j} - 5\mathbf{k})$		A1	
		State 3 equations in x , y , z , λ and μ		A1	
		Eliminate λ and μ		M1	
		Obtain answer $4x + 19y + 13z = 29$, or equivalent		A1	
	OR3:	Using a relevant point and relevant direction vectors,	form a determina		
		equation for the plane		M1	
		$\begin{vmatrix} x-1 & y-2 & z+1 \end{vmatrix}$			
		State a correct equation, e.g. $\begin{vmatrix} x-1 & y-2 & z+1 \\ 2 & 3 & -5 \\ 3 & -2 & 2 \end{vmatrix} = 0$		A1	
		·		3.61	
		Attempt to expand the determinant		M1	
		Obtain correct values of two cofactors Obtain answer $4x + 19x + 13x = 29$ or equivalent		A1	=
		Obtain answer $4x + 19y + 13z = 29$, or equivalent		A1	5